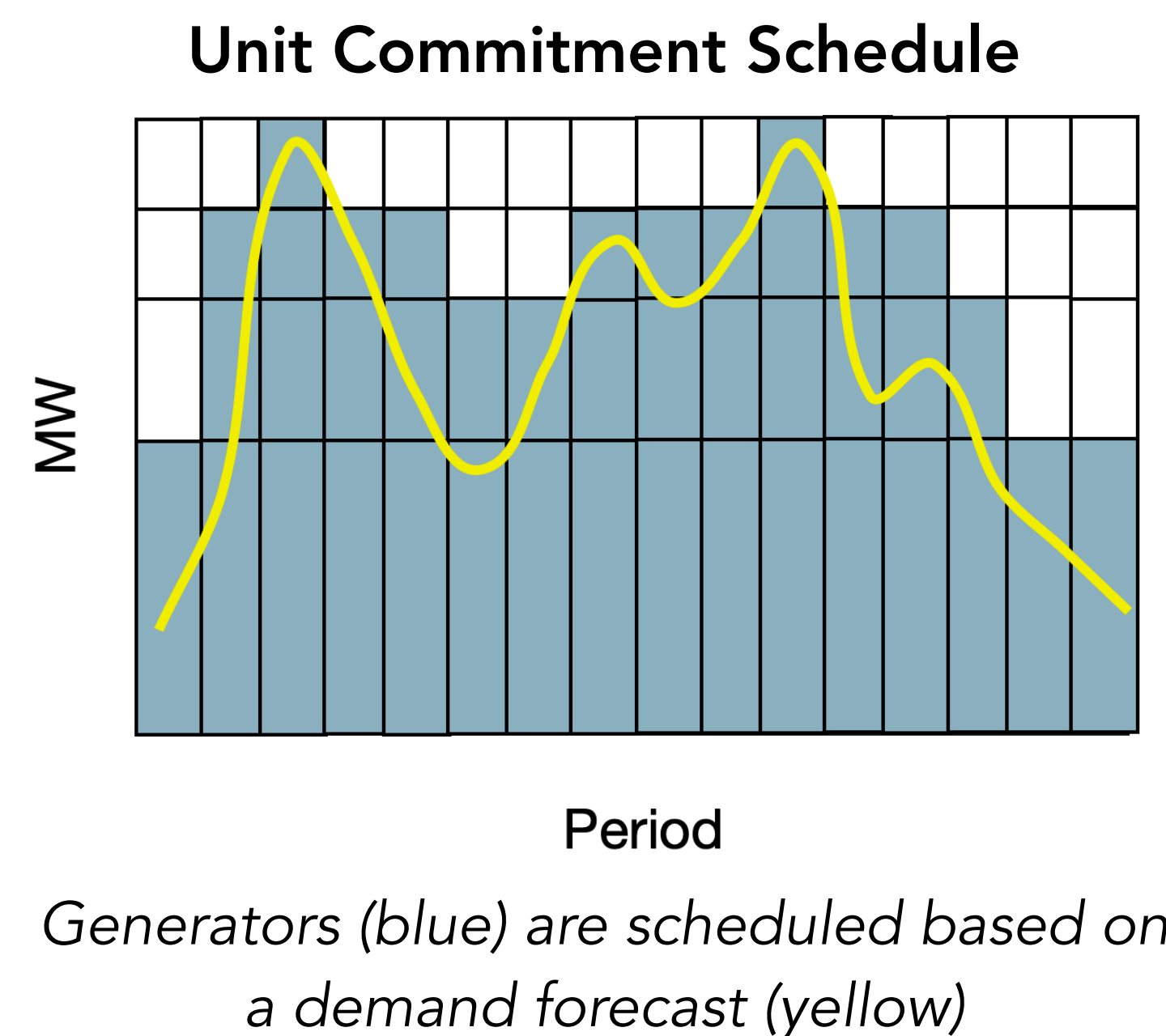


# Guided A\* Search for Scheduling Power Generation Under Uncertainty

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# The Unit Commitment (UC) Problem

- **Fundamental task in power systems operation:** determining on/off schedules of power generators for future period (e.g. day ahead)
- Objective: **minimise expected operating costs** over uncertain demand, wind and other stochastic processes
- Typically solved by mixed-integer linear programming (MILP) using a deterministic reserve constraint (e.g. proportion of demand or 'N-1' criterion) to manage uncertainty

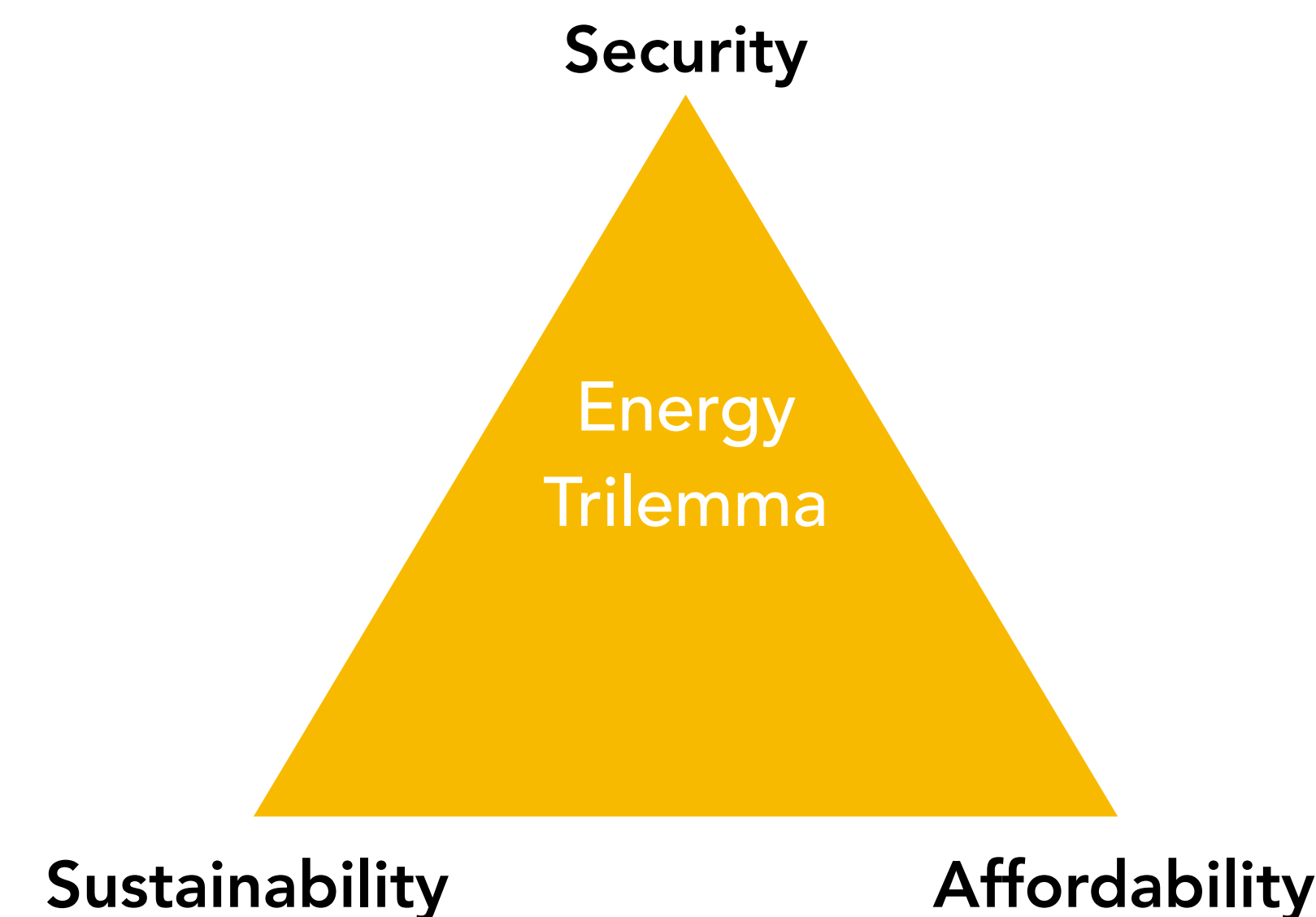


# Motivation

- Uncertainty increasing due to: renewables penetration, behind-the-meter generation, 'prosumers', electrification of end-use sectors etc.
- Deterministic approaches are sub-optimal in high uncertainty power systems [1]
- Scenario-based stochastic optimisation approaches are computationally expensive [2]
- Large and growing size of power systems means **small efficiency improvements of existing assets can result in large absolute CO<sub>2</sub> emissions reductions**

# Applying RL to the UC Problem

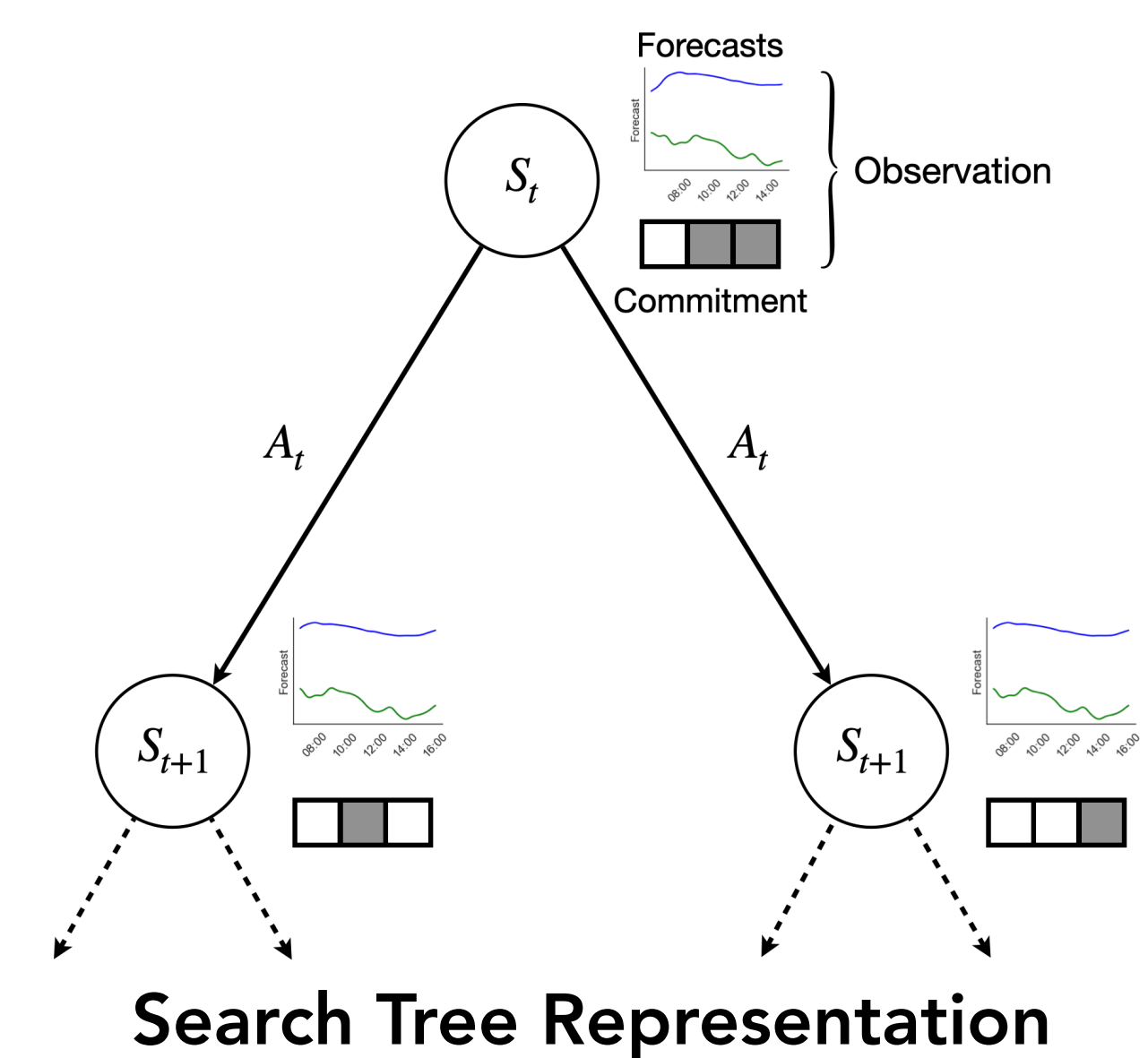
- RL is an attractive framework:
  - Suited to stochastic sequential decision making problems
  - Most of the computation (i.e. training) conducted in advance
  - Reward can be shaped to reflect societal values (**energy trilemma**)
- Challenges:
  - Large discrete (combinatorial) action space (up to  $2^N$  actions)
  - Extreme penalties for lost load (blackouts), requiring **safe operation**
  - **Long time dependencies** (generators cannot be switched on/off frequently)
- **Existing research has only considered small power systems** (up to 12 generators) and hasn't considered generalisability to unseen problems (training and testing on same profiles)



# UC as a Markov Decision Process

- We formulate the UC problem as an episodic MDP with  $T$  decision periods and  $N$  generators
- Agent observes forecasts and current generator up/down times; actions are **combinatorial commitment decisions**
- **Stochastic demand and wind** modelled as auto-regressive moving average (ARMA) processes
- Reward reflects operating cost comprised of: fuel cost, carbon cost, startup cost, lost load cost (penalty for blackouts)
- Search tree representation: replace edge costs with expected cost using Monte Carlo approach
  - Solve the UC problem by finding lowest cost path
  - Note:  $2^N$  branches for  $N$  generators!

<b>States</b>	$u_t$ : generator up/down times $\in \mathbb{Z}^N$ $d$ : demand forecast $\in \mathbb{R}^T$ $w$ : wind forecast $\in \mathbb{R}^T$ $x_t$ : demand forecast error $\in \mathbb{R}$ $y_t$ : wind forecast error $\in \mathbb{R}$ $t$ : timestep $0 \leq t \leq T \in \mathbb{Z}$
<b>Observations</b>	$\{u_t, d, w, t\}$
<b>Actions</b>	$a_t$ : commitment decisions $\{0, 1\}^N$
<b>Rewards</b>	$r_t$ : negative operating cost $\in \mathbb{Z}$
<b>Transitions</b>	$u_{i,t+1} = \begin{cases} u_{i,t} + 1, & \text{if } a_{i,t} = 1 \text{ and } u_{i,t} > 0 \\ 1, & \text{if } a_{i,t} = 1 \text{ and } u_{i,t} < 0 \\ -1, & \text{if } a_{i,t} = 0 \text{ and } u_{i,t} > 0 \\ u_{i,t} - 1, & \text{if } a_{i,t} = 0 \text{ and } u_{i,t} < 0 \end{cases}$ $x_t \sim X_t$ : sample demand forecast error (from ARMA) $y_t \sim Y_t$ : sample wind forecast error (from ARMA)



# Solution Method: Guided A\*

- Train a policy  $\pi(a | s)$  using model-free RL (PPO)
- **Guided expansion** used to reduce search breadth, pruning low probability branches:

$$A_{\pi}(s) = \{a \in A(s) | \pi(a|s) \geq \rho\}$$

$\pi(a | s) :=$  expansion policy  
 $\rho :=$  branching threshold

- Use A\* search [3] with a **priority list heuristic** to find lowest cost path through tree to fixed depth  $H$
- In practice the UC problem is time constrained. We used iterative-deepening A\* (IDA\*) [4] as an anytime algorithm: incrementally increase  $H$ , terminate when time budget is spent

## Priority List Heuristic

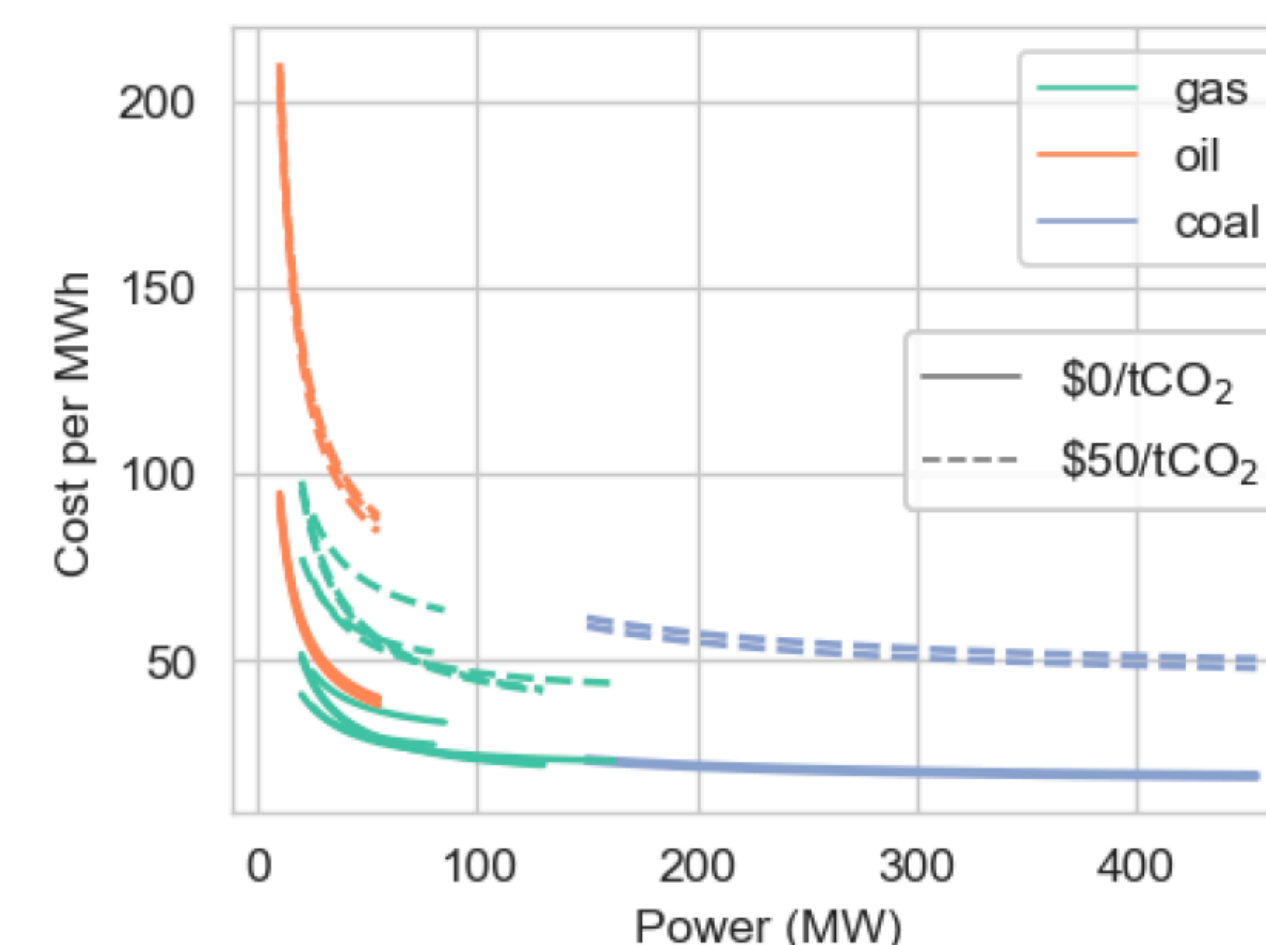
- A\* can exploit a problem-specific heuristic to improve search efficiency
- PL heuristic: commit generators in order of cost; ignore most constraints to improve speed



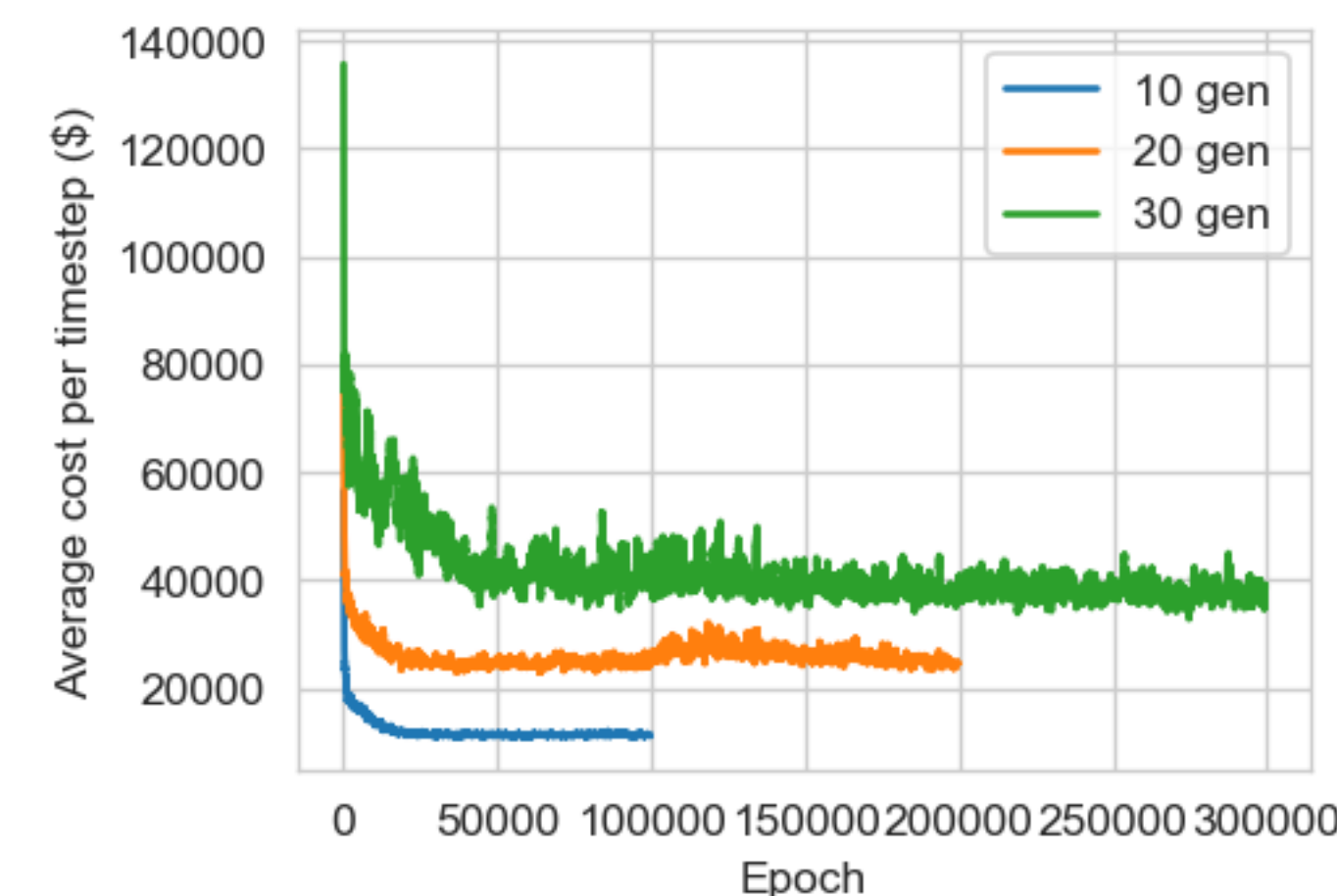
# Experimental Setup

- Experiments conducted on power systems of 10, 20 and 30 generators considered, based on data from [5] (widely used UC benchmark)
- Demand and wind forecasts based on GB power system data (4 years of training data with 20 held out days for testing)
- MDP represented in a Gym-style environment (<https://github.com/pwdemars/rl4uc>)
- Two experiments conducted:
  - Comparison with MILP with no carbon price
  - Impact of carbon price of \$50 per tCO<sub>2</sub>

Generator cost curves

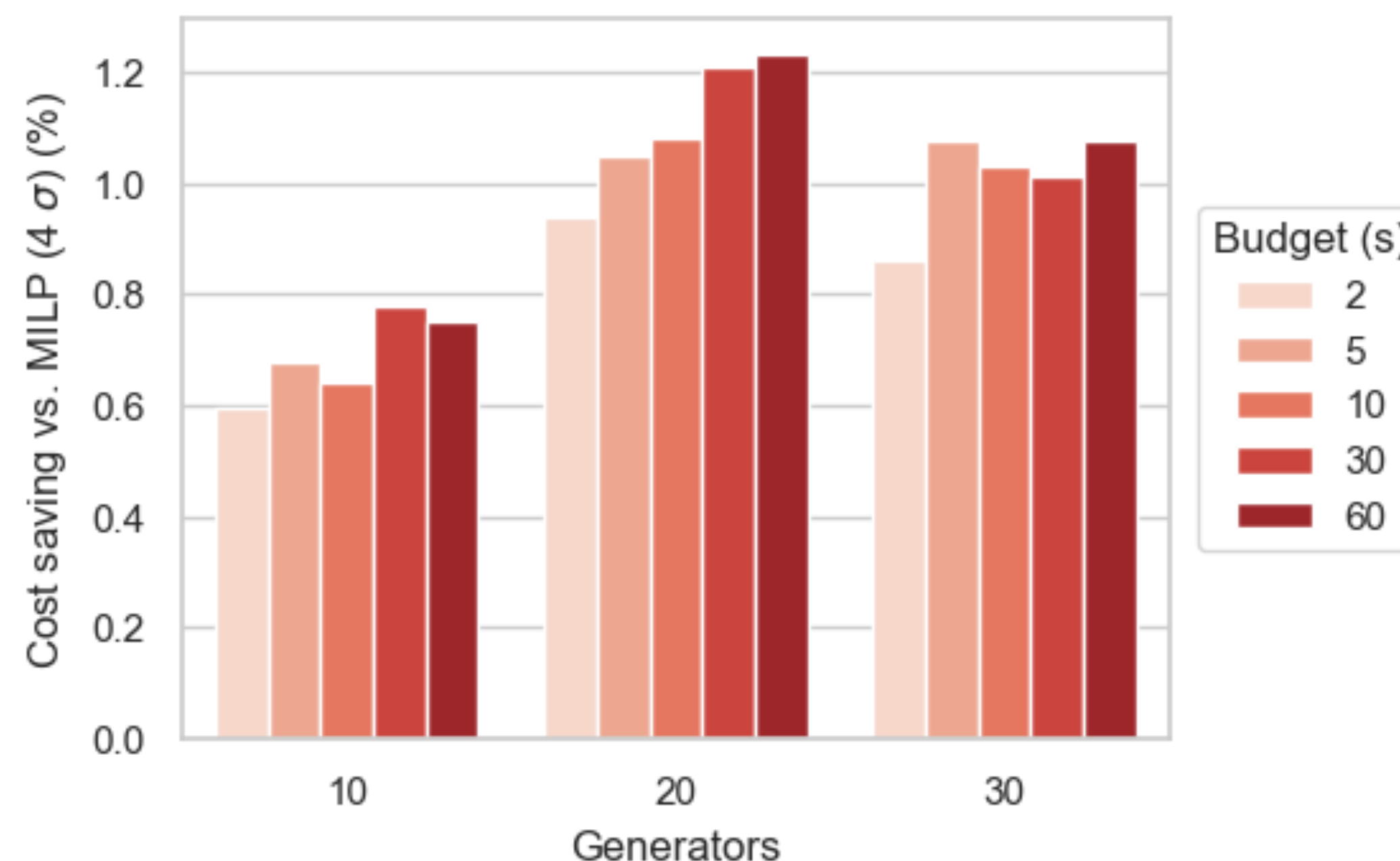


Policy training (PPO)



# Experiment 1: Guided A\* vs. MILP (no carbon price)

- Guided A\* schedules were **0.8—1.2% cheaper** than MILP with a deterministic reserve constraint
- Comparable to improvements of stochastic over deterministic MILP methods
- More secure operation: **loss of load probability roughly 50% lower** for guided A\* compared with MILP



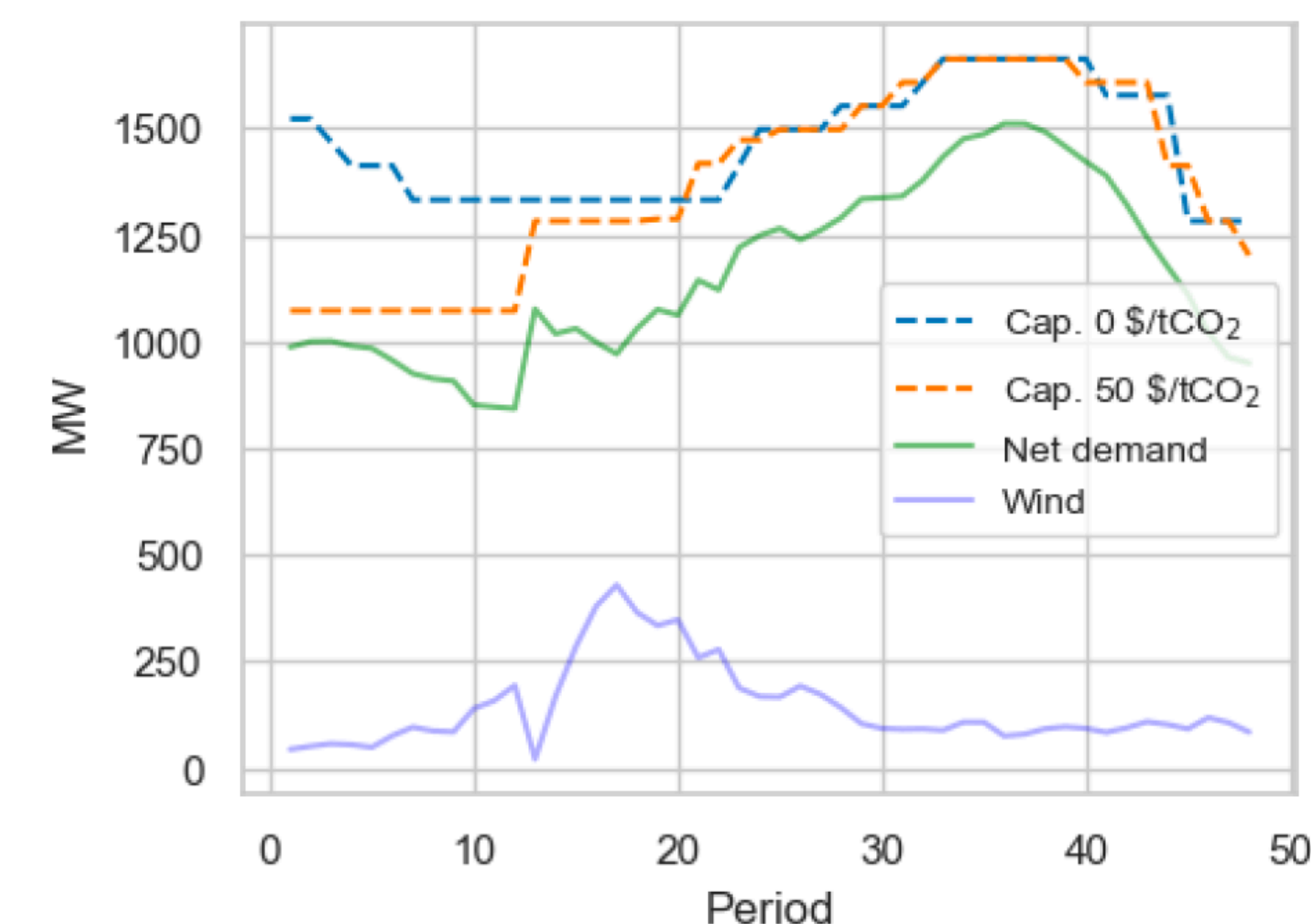
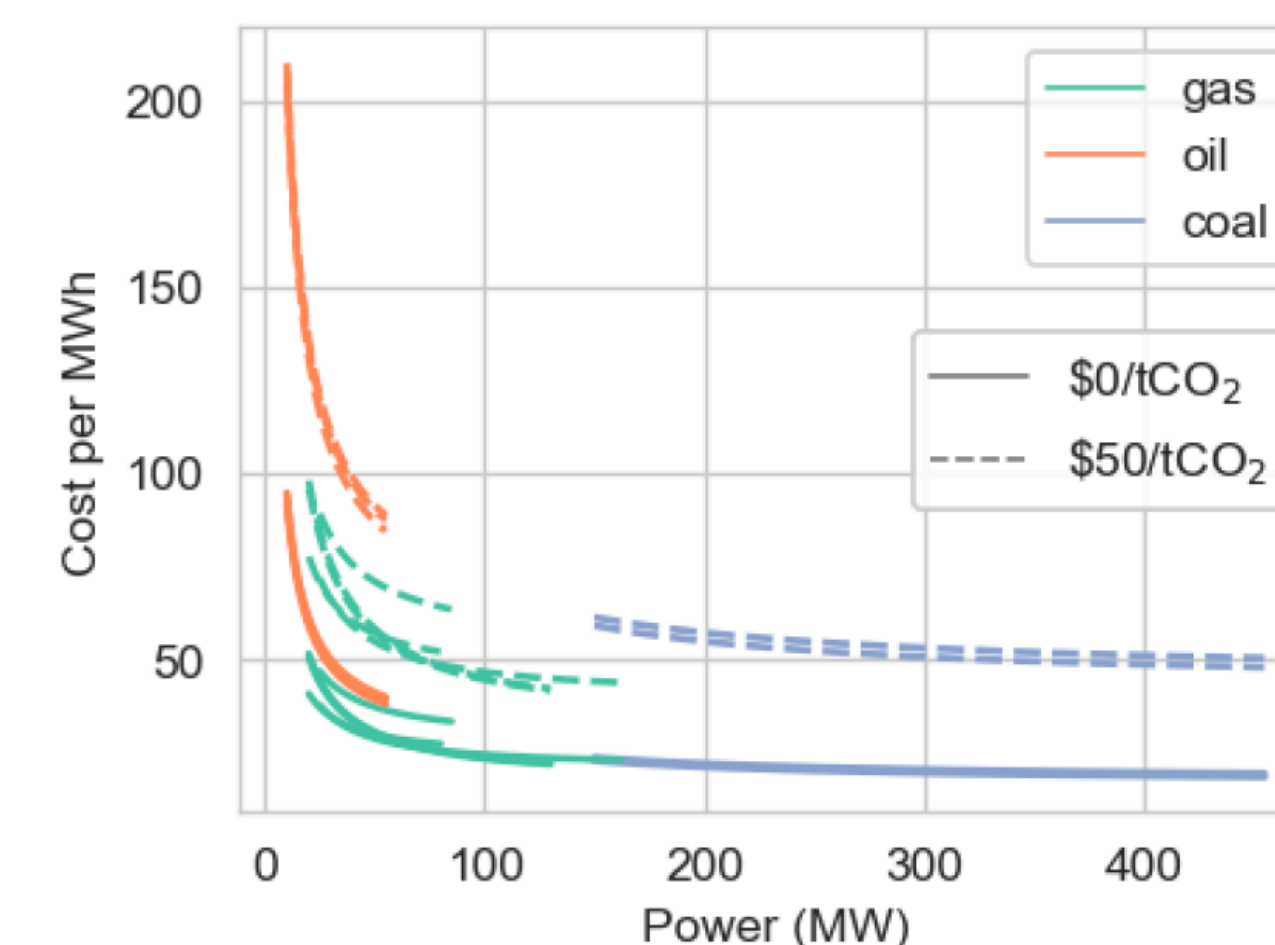


# Experiment 2: Guided A\* with Carbon Price

# Gens	\$/tCO <sub>2</sub>	LOLP (%)	ktCO <sub>2</sub>	Coal (%)	Gas (%)	Oil (%)	Startups
10	0	0.12	264.03	99.64	41.88	6.28	141
10	50	0.12	245.89	91.30	61.37	13.19	114
20	0	0.11	527.56	99.09	40.74	8.21	235
20	50	0.09	476.62	86.38	66.24	5.38	164
30	0	0.16	780.43	99.10	40.89	5.69	346
30	50	0.17	724.81	88.59	67.86	12.67	215

- Including a carbon price of \$50 per tCO<sub>2</sub> **reduces total carbon emissions by between 7—10%**
- Usage of generators (% periods online) shifts from coal towards lower carbon intensity generation (gas)
- Fewer startups, smaller reserve margins with carbon price

Generator cost curves



# Conclusions

- RL can be successfully applied to the UC problem when combined with planning methods
- Reward shaping significantly alters behavioural strategies
- RL for power systems requires domain expertise: methods can't be applied out-of-the-box!

Thank you for listening, please get in touch if you have any questions!

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# References

- [1] Ruiz, P. A., Philbrick, C. R., Zak, E., Cheung, K. W., and Sauer, P. W. Uncertainty management in the unit commitment problem. *IEEE Transactions on Power Systems*, 24 (2):642–651, 2009.
- [2] Bertsimas, D., Litvinov, E., Sun, X. A., Zhao, J., and Zheng, T. Adaptive robust optimization for the security constrained unit commitment problem. *IEEE Transactions on Power Systems*, 28(1):52–63, 2012.
- [3] Russell, S. and Norvig, P. *Artificial Intelligence: A Modern Approach*. Prentice Hall Press, USA, 3rd edition, 2009. ISBN 0136042597.
- [4] Korf, R. E. Real-time heuristic search. *Artificial Intelligence*, 42(2-3):189–211, 1990.
- [5] Kazarlis, S. A., Bakirtzis, A., and Petridis, V. A genetic algorithm solution to the unit commitment problem. *IEEE Transactions on Power Systems*, 11(1):83–92, 1996.