Fast-Slow Streamflow Model Using Mass-Conserving LSTM

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Abstract

Streamflow forecasting is key to effectively managing water resources and preparing for the occurrence of natural calamities being exacerbated by climate change. Here we use the concept of fast and slow flow components to create a new mass-conserving Long Short-Term Memory (LSTM) neural network model. It uses hydrometeorological time series and catchment attributes to predict daily river discharges. Preliminary results evidence improvement in skills for different scores compared to the recent literature.

1. Introduction

Streamflow forecasting is essential in the planning and operation of water resources, such as supplying cities, electricity production, irrigation, and navigation. It also helps to prepare for natural disasters, such as floods and droughts. Having accurate methods to predict river discharge in advance would help to manage uncertainties that affect society and the economy, a challenge under climate change.

In this paper, we consider the problem of predicting next day streamflow given time series of past meteorological data (precipitation, soil moisture, and temperature) and physiographic attributes, such as land cover type, soil, topography, etc, of the catchment. We assume to have access to river discharge measurements for a certain period to train/calibrate the streamflow model. Once trained, the model should run on meteorological and physiographic data only, i.e, without access to new streamflow data to update the model. This simulates a scenario where a river gauge station ceased to operate, which is consistent with the globally observed decline in station coverage (Gudmundsson et al., 2018).

In this paper we have three main objectives:

1. Propose a new LSTM architecture to estimate streamflow that implicitly modulate fast and slow flows components, respecting mass conservation.

We follow the approach of empirical modeling, focusing on machine learning. Past solutions vary from simple autoregressive models, such as multilinear regression (MLR) (Tangborn & Rasmussen, 1976), auto-regressive moving average (ARMA) (Box et al., 2015) and variations that attempt to model physical relations by using exogenous variables (ARMAX) (Haltiner & Salas, 2007). While simpler models offer a very good solution for streamflow forecasting, often they require pre-processing steps before model application, such as time series seasonal decomposition.

Black-box approaches of the kind of artificial neural networks (ANN) (Govindaraju, 2000), offers a straightforward alternative to model nonlinear hydrological relations. ANNs have been shown to outperform ARMA and MLR models (Cigizoglu, 2005). Under proper training, the prediction skill of many streamflow prediction approaches based on ANN improves as the flexibility (complexity) of the model increases, but at an increased computational cost to train.

Recently, Long Short-Term Memory (LSTM), a type of artificial recurrent neural network architecture that can store and forget information over time has shown promising results in streamflow modeling (Kratzert et al., 2019).

Mass conservation is an important property exploited to customize LSTM formulations to ensure certain inputs are conserved and redistributed across storage locations in a system (Hoedt et al., 2021). In Hoedt’s et al. application in hydrology, the amount of water is conserved using an LSTM variant with new neural arithmetic units that preserve a constant sum of memory cells over time. The LSTM architecture use two types of inputs: one related to mass, such as contributions to the streamflow, and auxiliary inputs, that variables control how the streamflow and these new contributions generate the next value of streamflow in a time series, acting as inputs to the gates that control mass fluxes.

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2. Improve the efficiency of streamflow modeling by us-
ing a projection layer in our LSTM architecture, thus encoding catchment attributes in a smaller data space.

3. Test the skill of our LSTM architecture to predict streamflow in 32 stream gauges located in southern Brazil, comparing results to state-of-the-art models.

2. Related work

2.1. Mass-Conserving LSTM

Hoedt et al. (2021) modified an LSTM to represent in a recurrent cell the dynamics of the water balance, by receiving water contributions \( Q \) (i.e. precipitation \( p \)). Their model was proposed to estimate streamflow using mass-conserving LSTM. We also take note of the mass-conserving LSTM model reviewed in Section 2.1 and build on these prior works.

\[
\begin{align*}
\mathbf{m}_t^{\text{tot}} &= \mathbf{R}^t \cdot \mathbf{c}^{t-1} + \mathbf{i}^t \cdot \mathbf{x}^t \quad (1) \\
\mathbf{c}^t &= (1 - \sigma^t) \odot \mathbf{m}_t^{\text{tot}} \quad (2) \\
\mathbf{h}^t &= \sigma^t \odot \mathbf{m}_t^{\text{tot}} \quad (3) \\
q^t &= \sum_{i=1}^{n-1} h_i^t 
\end{align*}
\]

where:

\[
\begin{align*}
\mathbf{i}^t &= \text{softmax} (\mathbf{W}_i \cdot \mathbf{a}_t + \mathbf{U}_i \cdot \tilde{\mathbf{c}}_t + \mathbf{b}_i), \\
\mathbf{o}^t &= \sigma (\mathbf{W}_o \cdot \mathbf{a}_t + \mathbf{U}_o \cdot \tilde{\mathbf{c}}_t + \mathbf{b}_o), \\
\mathbf{R}^t &= \text{softmax} (\mathbf{W}_r \cdot \mathbf{a}_t + \mathbf{U}_r \cdot \tilde{\mathbf{c}}_t + \mathbf{b}_r), \\
\end{align*}
\]

\( \tilde{\mathbf{c}}_t \) is a normalization of \( \mathbf{c}_t \). This simple model reasonably approximated streamflows in warm seasons. However, large biases were observed during periods of high rainfall (Koster et al., 2018).

2.2. Fast and slow components of streamflow

Koster et al. (2018) proposed a simple model to predict 10-day streamflow totals in medium-sized watersheds using only average precipitation and soil moisture of the basins. Their model was proposed to estimate streamflow using only data from the Soil Moisture Active Passive (SMAP) satellite mission. According to the authors, streamflow can be approximated by fast and slow flow components. The fast flow \( Q_{\text{fast}} \) portion of precipitation \( p \) is proportional to the soil moisture \( w \) of the top surface layers of the soil (i.e., \( Q_{\text{fast}} \propto w \cdot p \)), and the slow flow is \( Q_{\text{slow}} \propto w \). These relations can be combined to represent the dynamics of streamflow \( Q \) as a quadratic function of \( p \) and \( w \):

\[
Q = Q_{\text{fast}} + Q_{\text{slow}} = \alpha \cdot w \cdot p + \beta \cdot w + \gamma \quad (8)
\]

This means that instead of relying on the simple streamflow model considered in (3), we account for possible nonlinearities in streamflow using a multilayer perceptron neural network \( L(w^t, p^t) \), that takes as inputs precipitation and soil moisture and output the unknown fast and slow flow components. Assuming that the relation between precipitation and soil moisture (modulating between fast and slow flow components) is close to the quadratic function proposed by (Koster et al., 2018) shown in (8), we decided to use a relatively smaller number of layers and neurons in the network \( L(w^t, p^t) \) shown in Figure 1. To ensure positive values of \( L(w^t, p^t) \) we use a quadratic function at the output layer. Also, using (2) and (3) to determine \( \mathbf{c}^t \) and \( q^t \), we have that:

\[
\begin{align*}
\mathbf{r}^t &= \mathbf{W}_r \cdot \mathbf{a}_t \\
\mathbf{i}^t &= \text{softmax} (\mathbf{W}_i \cdot \mathbf{r}^t + \mathbf{U}_i \cdot \tilde{\mathbf{c}}_t + \mathbf{b}_i) \\
\mathbf{o}^t &= \sigma (\mathbf{W}_o \cdot \mathbf{r}^t + \mathbf{U}_o \cdot \tilde{\mathbf{c}}_t + \mathbf{b}_o) \\
\mathbf{R}^t &= \text{softmax} (\mathbf{W}_r \cdot \mathbf{r}^t + \mathbf{U}_r \cdot \tilde{\mathbf{c}}_t + \mathbf{b}_r)
\end{align*}
\]

Differently from the MC-LSTM model, we propose to use...
We also included in the analysis soil moisture from gridded GLDAS (Rodell et al., 2004) version 2.0. This product provides the surface soil moisture daily average in kg/m² for the top 10-cm soil layer. We compute daily average soil moisture values using the polygon data available in the shapefiles (available in (Chagas et al., 2020a)) that delineate the catchment of each stream gauge station.

As $L(\cdot)$ input variable, we use the average of precipitation in the catchment, in mm/day, derived from CHIRPS (Funk et al., 2015), that is distributed with CAMELS-BR. The auxiliary dynamic input variables were the minimum, mean, and maximum temperatures from NOAA (Climate Prediction Center, 2019). The static variables, used to characterize the catchment, are: elevation mean, slope mean, area, forest percentage, bedrock depth, water table depth, sand percentage, silt percentage, clay percentage, geological permeability, pressure mean, potential evapotranspiration mean, aridity, high precipitation frequency, high precipitation duration, low precipitation frequency and low precipitation duration.

4.2. Evaluation criteria

We use six scores that attempt to capture different skills sought in streamflow predictions. The Nash–Sutcliffe model efficiency coefficient (NSE) (Nash & Sutcliffe, 1970) that helps to understand how the model improves over the mean. The Kling–Gupta Efficiency (KGE) (Gupta et al., 2009) which is a weighted sum of the three components that appear in the NSE formula: linear correlation, variability ratio, and bias ratio. The root mean squared error (RMSE). We also use three scores derived from the flow duration curve (FDC), a cumulative frequency curve that shows the percent of time specified discharges were equaled or exceeded during a given period (see examples in Figure 5). The bias of the high-segment volume ($\% \text{BiasFHV}$) with exceedance probabilities 0.0-0.2, the mid-segment slope ($\% \text{BiasFMS}$ in 0.2-0.7, and the low-segment volume ($\% \text{BiasFLV}$) in 0.7-1.0 (Yilmaz et al., 2008).
4.3. Experimental set-up

All stations shared in common daily time series from 1 October 1994 to 30 September 2008. We trained on streamflow observations from 1 October 1999 to 30 September 2008 and tested on observations from 1 October 1994 to 30 September 1999. The remaining initial observations (1 October 1990 to 30 September 1994) were set aside for validation during the training to avoid over-fitting problem.

We compared our FS-LSTM model to three alternative methods: a vanilla LSTM (Kratzert et al. 2018); EA-LSTM (Kratzert et al. 2019), in both cases the meteorological forcing data and additional catchment attributes controls the state space that are used; and MC-LSTM (Hoedt et al. 2021) considered state-of-the-art. The common setup configuration for all the lstm architectures is shown in Table 1.

In this table, the input size includes the number of previous time steps of mass, and auxiliary catchment variables that are needed to forecast the streamflow output. For the ANN architecture shown in Figure 1 we used 2 layers and 10 neurons per layer. Also for we used \( n_r = 10 \) that respect (14). In our experiments with MC-LSTM, we set soil moisture as an input mass variable, not originally considered in (Hoedt et al. 2021). Each model trains with all gauges pooled together in 30 epochs.

4.4. Results

The charts in Figure 4 illustrate the kernel density estimates for the six scores evaluated in the 32 basins during the testing period. The proposed FS-LSTM outperforms the alternative algorithms tested in terms of NSE, with an average of 0.7 compared to 0.68 of EA-LSTM, ranked second, and 0.66 of the vanilla LSTM, with relatively higher standard deviations. A relative improvement (RI) of 2.9%. FS-LSTM achieved the lowest average RMSE error of 1.43 mm/day, compared to 1.51 mm/day (5.3% RI) of EA-LSTM, all having similar density curves. In terms of KGE, the advantage of FS-LSTM also becomes clear, with a density curve shifted towards higher values, with an average of 0.79 compared to the 0.77 (2.6% RI) of the vanilla LSTM.

Results are more mixed for the scores based on the FDC. MC-LSTM outperforms the other methods in terms of average %BiasFHV, but we note that all models perform well since most of their densities values have bias within the ±25% range recommend by (Moriasi et al. 2007). With %BiasFMS, arguably the proposed FS-LSTM has the second overall performance because the kernel density curve looks more symmetrical around zero and only a small portion of the tales are outside the target ±25% bias bound. For the %BiasFLV, our experiments suggest that FS-LSTM and EA-LSTM perform very well compared to MC-LSTM and LSTM, attaining the desired ±25% bound.

Figure 5 presents two examples of FDC for the gauges with the worst (left) and best (right) NSE.

5. Conclusions

The approach proposed herein exploits a novel strategy that uses a multilayer perceptron artificial neural network to implicitly model the fast and slow streamflow components in a modified mass-conserving LSTM. We demonstrate that the proposed FS-LSTM achieves high prediction skill for gauges located in southern Brazil. Improvements in the low streamflow volumes remain a challenge, as well as the investigation of strategies to transfer these models to other geographies with less retraining effort.
References


